

Hypothetical Lorentz invariance violation and the muon content of extensive air showers

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What problem are we solving?

Many experiments have observed an unexplained excess of muons in extensive air showers (EASs). This phenomenon is known as the '*muon puzzle*'—an open question in science.

The muon excess is often parametrized by the variable

$$z \equiv \frac{\ln \langle N_{\mu}^{\text{obs}} \rangle - \ln \langle N_{\mu,p}^{\text{MC}} \rangle}{\ln \langle N_{\mu,Fe}^{\text{MC}} \rangle - \ln \langle N_{\mu,p}^{\text{MC}} \rangle}$$

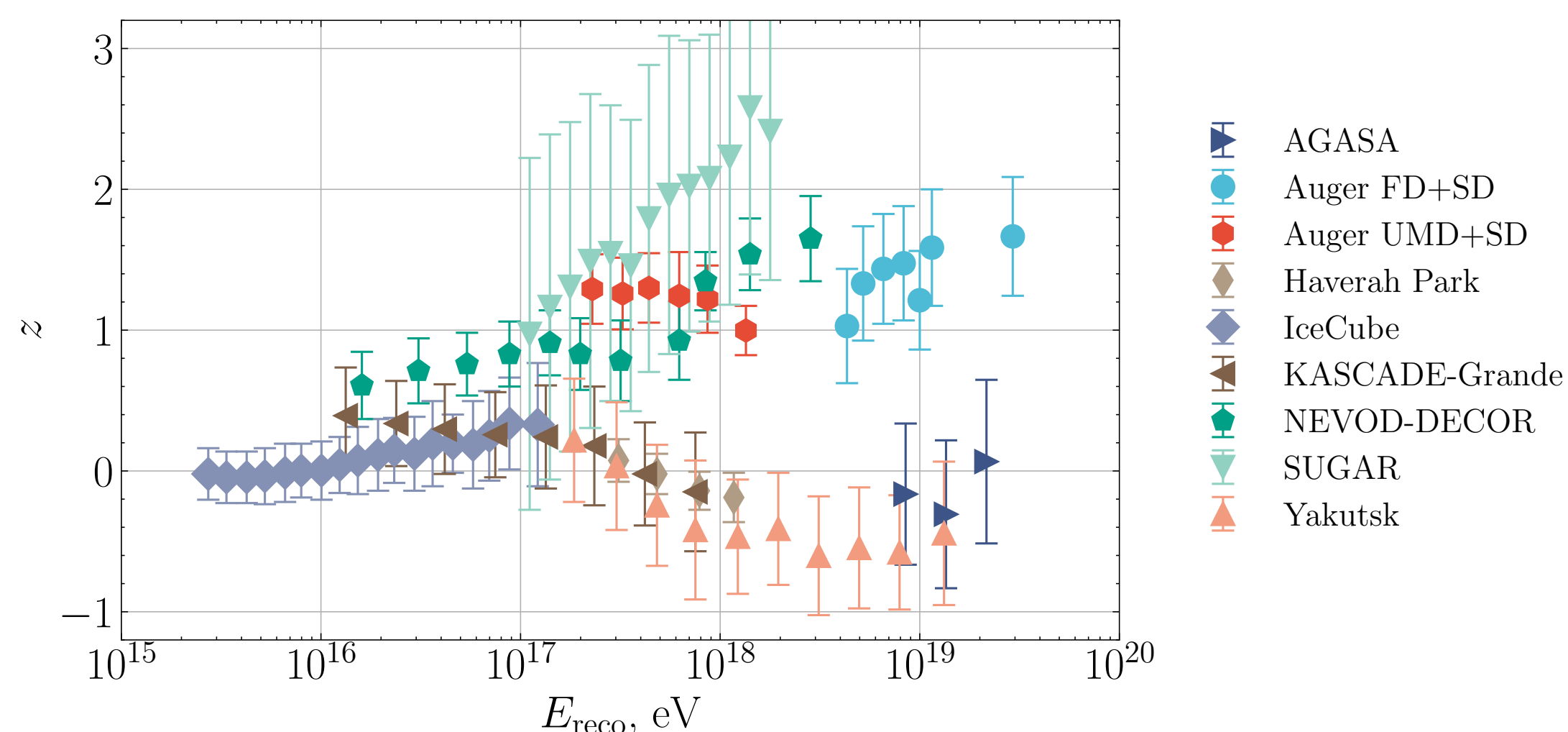
the mean value of the measured muon density

the mean value of the predicted muon density by Monte-Carlo simulations for proton-ray nucleus

the mean value of the predicted muon density by Monte-Carlo simulations for iron-ray nucleus

all dots should be kept in the region between $z=0$ and $z=1$!!!

Experimental data:



How to solve the muon puzzle? — Of course, let's modify the SM!

Let's modify, especially, the QED sector:

$$\mathcal{L} = \mathcal{L}_{\text{QED}} + \mathcal{L}_{\gamma},$$

where the following term modify the dispersion relation:

$$\mathcal{L}_{\gamma} = \frac{s_2}{4M_{\text{LIV}}^2} F_{kj} \partial_i^2 F^{kj},$$

and we get

$$E_{\gamma}^2 = k_{\gamma}^2 - \frac{k_{\gamma}^4}{M_{\text{LIV}}^2}.$$

the mass scale parameter for LI breaking

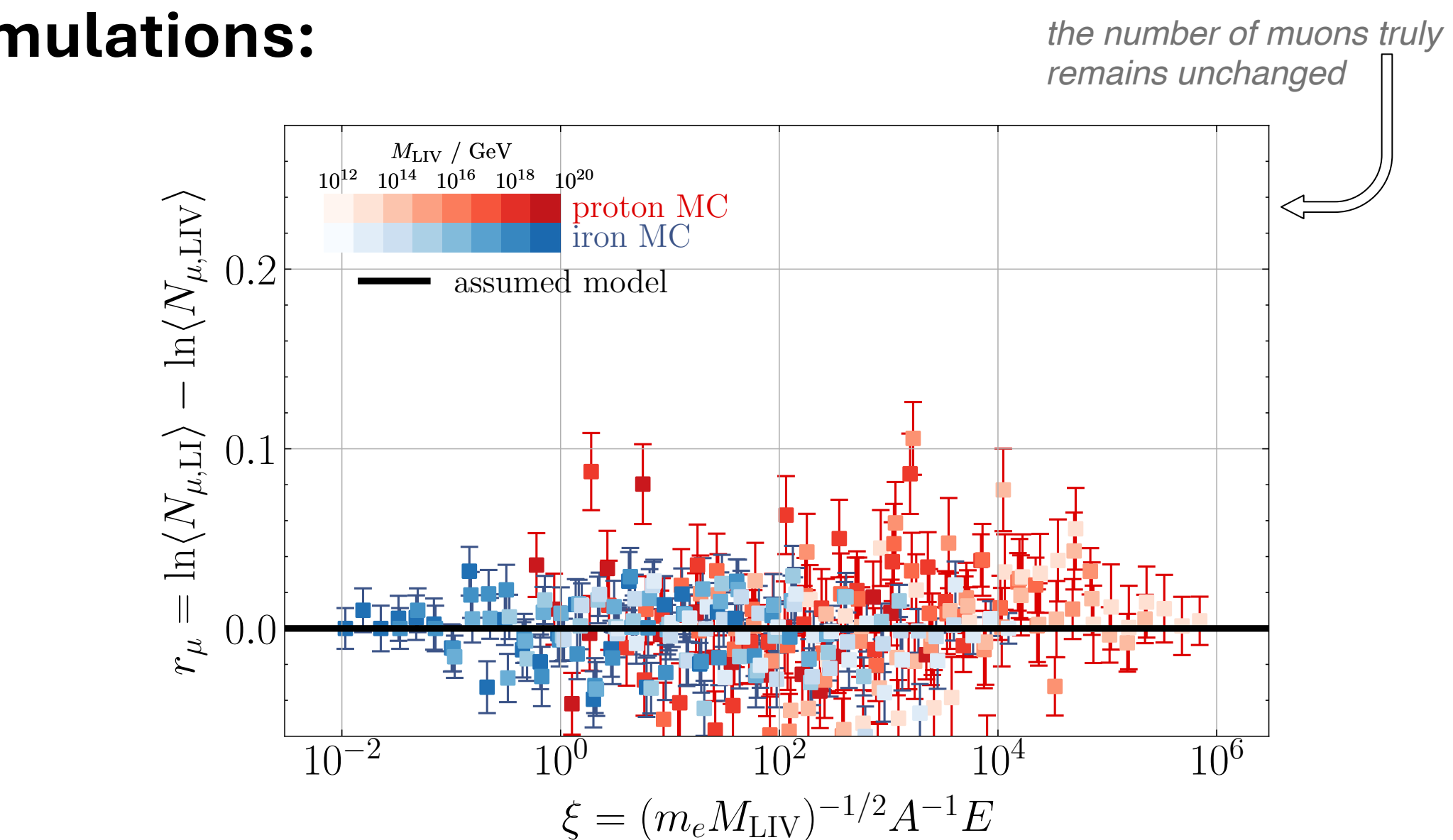
How does this theory affect EAS behavior?

Such a theory significantly changes the cross section in the photon-induced pair production reaction on a nucleus:

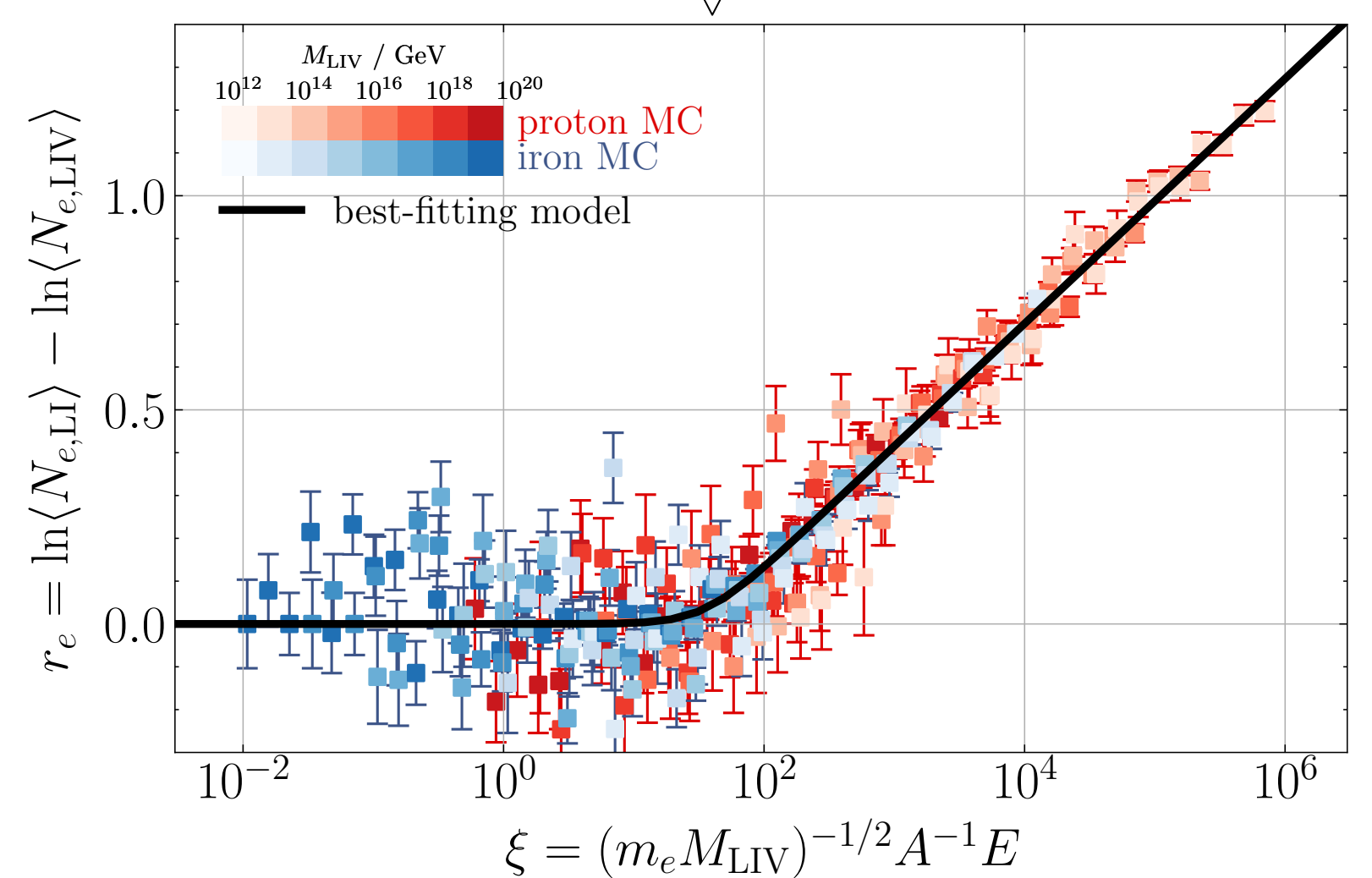
$$\frac{\sigma_{\text{BH}}^{\text{LIV}}}{\sigma_{\text{BH}}^{\text{LI}}} \simeq \frac{12m_e^2 M_{\text{LIV}}^2}{7E_{\gamma}^4} \times \log \frac{E_{\gamma}^4}{2m_e^2 M_{\text{LIV}}^2}$$

Key idea: The number of produced electrons decreases, which leads to incorrect reconstruction of the primary particle's energy, consequently resulting in an underestimation of the muon density.

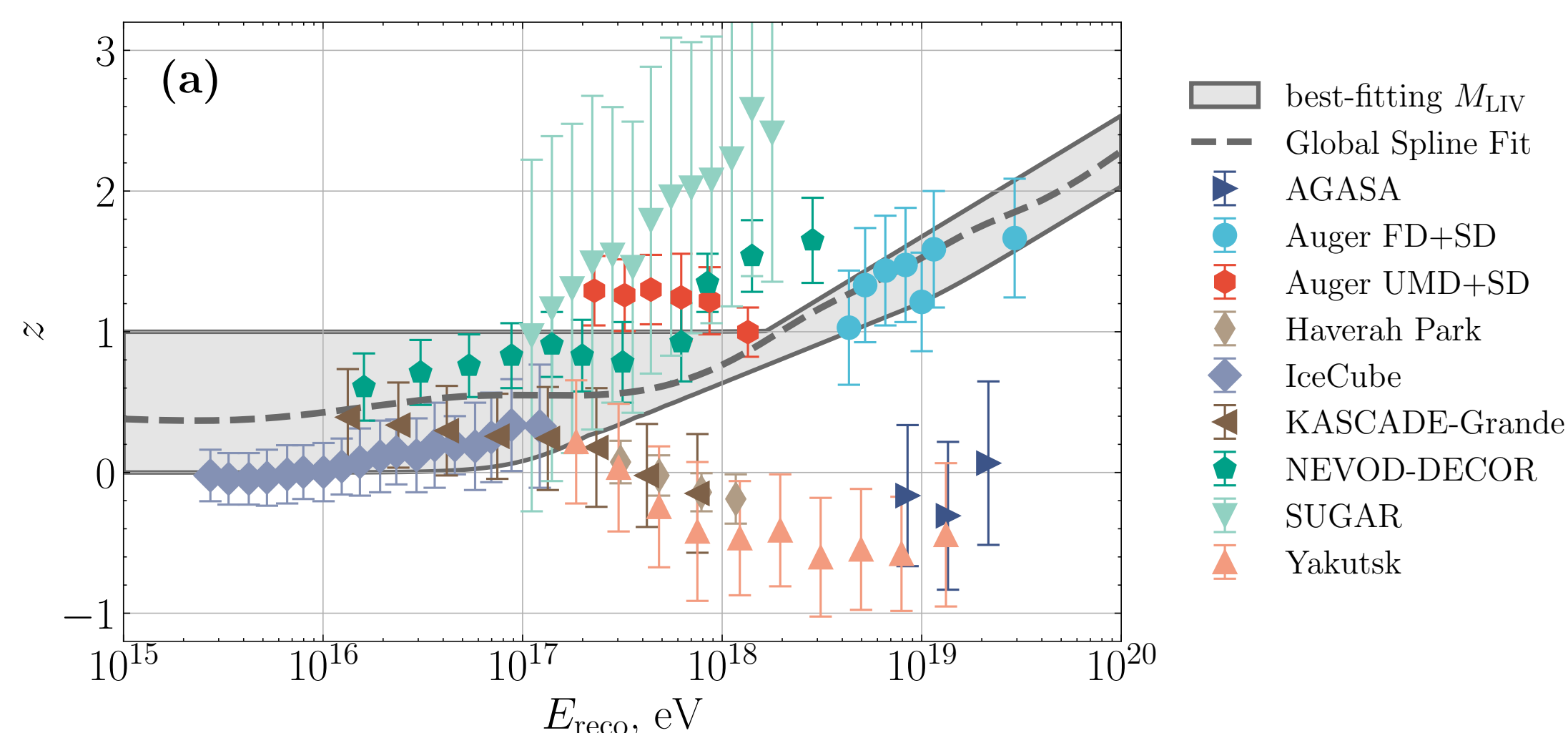
Simulations:



the number of electrons indeed decreases with increasing energy



Results:



We have shown that a subluminal LIV in the photon sector on the mass scale of $M_{\text{LIV}} \sim 10^{16}$ GeV could be an explanation for the muon puzzle!

Where to read about this:

1. arXiv: 2412.08349 — this work (and see PRD publication),
2. PoS ICRC2023 (2023) 466 — review by the WHISP group on the muon puzzle,
3. arXiv: 0802.1561 — on the test of Lorentz invariance violation (my personal recommendation).